

# Combined High Resolution UV and Microwave Results: Structure of the Benzonitrile-Water Complex

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High resolution ultraviolet (UV) and molecular beam Fourier transform microwave (MB FTMW) spectroscopy of the benzonitrile-water (BZNW) cluster were performed to measure cluster structures in the  $S_0$  and  $S_1$  states. The MW experiments provide additional information on the structure and the  $^{14}\text{N}$ -nuclear quadrupole coupling in the ground state  $S_0$ , the UV experiments on the dynamics in  $S_1$ .

The rotationally resolved sub-Doppler UV spectra of BZNW were measured by mass-selective resonance-enhanced two-photon ionization. For the first time this UV technique has been applied to hydrogen-bonded clusters. From the UV spectra the rotational constants are obtained by Correlation Automated Rotational Fitting. The MW spectra were analyzed with the model of a centrifugally distorted rotor including nuclear quadrupole coupling. A  $r_0$ -fit of the water position within the cluster is performed. The water is found to be located with its oxygen nearly in the plane of benzonitrile (BZN). For  $S_0$  ( $S_1$ ), the distance of the oxygen to the ortho hydrogen is  $r_0 = 2.477(4)$  Å ( $2.457(2)$  Å) and the angle to the ortho carbon-hydrogen bond  $143.34(2)^\circ$  ( $141.91(3)^\circ$ ). The structure differences in  $S_1$  and  $S_0$  can be explained by the structure changes of the BZN molecule. A line broadening, which points to a faster decay in  $S_1$  upon clustering with the polar solvent, is observed for the BZNW cluster.

## I. Introduction

The structure of benzonitrile-water ( $\text{C}_6\text{H}_5\text{CN}\cdot\text{H}_2\text{O}$ , BZNW) in the electronic ground and excited state has been a matter of current interest [1, 2]. The prototype system of water loosely bound to a cyano group allows the investigation of the fundamental properties of a hydrogen bonding between water and aromatic molecules. Our research is not only motivated by the recent experimental results on the clustering of benzonitrile (BZN) [1–5], benzene and related molecules [6–8], but also by the theoretical prediction of a twisted internal charge transfer reaction (TICT) [9, 10] in BZN. The charge transfer is expected to be influenced by the solvent [11, 12] and has been the subject of recent experiments with lower resolution for the related aminobenzonitriles [13–15].

The bonding distance is expected to affirm the character of the bonding. The main contribution is from hydrogen bonding, but due to the large permanent dipole moment of BZN of 4.18 debye [16] an influence of the dipole-dipole interaction on the bonding is expected different from the hydrogen bonding recently investigated in phenol-water [6] and pyridone-water [8].

The combination of results from the MW and mass-resolved UV experiments with rotational resolution joins the virtues of the two techniques and is shown to result in a successful structure determination. High resolution resonance enhanced two-photon experiments can resolve the rotational structure of a vibronic transition for a species with defined mass within all clusters present in the molecular beam. By fitting the data some predictions about the structure can be made. The gained predictions are not exact, but they can be used as approximate input for MW experiments, so that the search and assignment of rotational transitions is possible and leads to accurate ground state

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rotational constants. These results allow the exact interpretation of the UV experiments leading to detailed information about the  $S_1$  electronically excited state.

## II. Experimental

### A) Microwave Experiments

The microwave experiments were performed in Kiel using molecular beam (MB) Fourier transform microwave (FTMW) spectrometers with a resonator operating in the  $TE_{01}$  ( $H_{01}$ ) mode of a cylindrical cavity in the range 1 to 4 GHz [17] and a Fabry-Perot resonator operating from 7 to 26.5 GHz [18]. BZN,  $C_6H_5CN$ , supplied by Fa. Aldrich, Steinheim, was kept upstream the beam nozzle in a small vessel. The surface of the liquid substance was exposed to a stream of argon or preferably helium containing about 0.5 % of water vapour. A sample of 70 % enriched  $H_2^{18}O$ , which was used to gain more information about the structure was supplied by Cambridge Isotope Laboratories. A backing pressure of 120 kPa was used. Additional measurements in the region between 4 and 8 GHz were performed in Aachen, with a MB FTMW spectrometer described in [19]. First the spectrometers were used in the scan mode, see [19], to locate the transitions. These were afterwards recorded in the high resolution mode with 8 K sample points at a sample distance of 10 ns or 40 ns. From 0.5 to 16 K measuring cycles were necessary to obtain a good signal to noise ratio.

### B) UV Experiments

The UV experiments were performed in Munich. For the measurements, 5 bar backing pressure of Ar and 10 mbar of water were expanded supersonically through a specially developed heated ( $60^\circ C$ ) reservoir of fluid BZN just in front of a pulsed valve (modified Bosch) with a 200  $\mu m$  orifice. The experimental apparatus for the recording of high resolution UV spectra by mass-selected resonance-enhanced two-photon ionization was described in detail in our previous work [20]. Briefly, the light of an  $Ar^+$ -laser (Spectra Physics 171) pumps a cw single-mode ring dye laser (Coherent CR 699/29, Rhodamine 110). Its output is pulsed amplified in three XeCl excimer laser (Lambda Physik MSC 201) pumped amplifier stages operating with the dye Coumarine 307 [21]. After frequency doubling, the UV pulses have a duration of 10 ns (FWHM). In the present experiment the pulse

energy was reduced by transmission filters to 0.2 mJ. The frequency width of the laser light is 70 MHz (FWHM), which is close to the Fourier transform limit. For the second photon absorption step leading to ionization the light of a commercial XeCl excimer laser-pumped broad band dye laser (Lambda-Physik FL 2002, Coumarin 102) is frequency doubled and directed perpendicularly to the molecular beam counterpropagating to the excitation laser beam. The light pulses of the ionization laser have an energy of 0.2 mJ and a duration of 10 ns.

The mass selective detection of the produced ions is realized by a home-built linear time of flight mass spectrometer. A gated boxcar integrator (Stanford Research Systems SR250) integrates the signal of the channel plates in the appropriate time window, a microcomputer (Force CPU-37) controls the laser frequency and records the signal intensity and the calibration signals.

Simultaneously recorded were the calibration signals with fractions of the visible cw laser light. The relative frequency calibration signal is provided by a 150 MHz Fabry-Perot interferometer transmission spectrum, and the absolute frequency calibration signal by an iodine vapor fluorescence excitation spectrum, which is positioned according to [22, 23].

## III. Results and Discussion

The shape of the UV spectrum, which is described in detail below, provides a first qualitative estimate of the structure. The orientation of the dipole transition moment with respect to the principal axes of the cluster makes up the shape of the spectrum due to the specific selection rules. The selection rules can be stated by means of  $K_a$  and  $K_c$ , the quantum numbers of rotation about the  $a$  and  $c$  axes in the limiting cases of the corresponding prolate and oblate symmetric tops. If the transition moment is oriented parallel to the  $a$ -axis the selection rules  $\Delta K_a = 0, \pm 2, \dots$  and  $\Delta K_c = \pm 1, \pm 3, \dots$  apply. For a position parallel to the  $b$ -axis  $\Delta K_a = \pm 1, \pm 3, \dots$  and  $\Delta K_c = \pm 1, \pm 3, \dots$ , for a position parallel to the  $c$ -axis  $\Delta K_a = \pm 1, \pm 3, \dots$  and  $\Delta K_c = 0, \pm 2, \dots$  apply. For any other position of the transition moment contributions from the three projections on the principal axes determine the relative intensities of the transitions [24]. For pure  $a$ - or  $b$ -type transitions the spectrum will consist of two broad wings with basically a hole in the middle. On the other hand if the transition moment is oriented parallel to the  $c$ -axis

the spectrum would consist of two broad wings and a sharp central peak outranging the side wings.

For the BZN monomer the orientation of the transition moment parallel to the *b*-axis is known [3]. As is known from high resolution spectroscopy of other clusters, the orientation of the transition moment is only slightly affected by clustering, but the direction of the main axes of the moment of inertia tensor is changed. Therefore a position of the water above the ring would change the spectrum to *c*-type and the *b*-axis of the BZN monomer would become the *c*-axis of the cluster like in the case of BZN·Ar [3]. On the other hand, a position of the water in the plane of BZN would only turn the *b*-axis of the monomer within the *a*-*b*-plane and a mixed *a*- and *b*-type spectrum is expected.

The latter is indeed the kind of spectrum we observe, and therefore the oxygen of the water must be located near the BZN plane in contrast to benzene-water [25] or BZN·Ar [3, 4], where the water or argon, respectively, is positioned above the ring. This can be concluded from the highly resolved UV spectrum without a detailed analysis of its rotational structure. This is the starting point for the MW experiment.

#### A) Analysis of the Microwave Spectra

The data from the initial UV experiments provided starting values for the rotational constants in a range of about 150 MHz maximum within the final constants. After scans [26] covering regions of about some 100 MHz transitions of the BZNW cluster could be identified. It was of great help, that the BZN rotational spectrum was thoroughly investigated (Table 3 of [4], [27]). The cluster lines assignment was verified by an analysis with the model of a centrifugally distorted asymmetric rotor [28] using the program ZFAP4 [29]. In addition the  $^{14}\text{N}$ -hyperfine structure (hfs) could be analyzed with high accuracy [30]. The program HFS [31, 32] was used in order to confirm the assignment. Following this procedure two isotopomers,  $\text{C}_6\text{H}_5\text{CN}\cdot\text{H}_2^{16}\text{O}$  and  $\text{C}_6\text{H}_5\text{CN}\cdot\text{H}_2^{18}\text{O}$ , were studied. The lines are given in Table 1 and Table 2 and the resulting rotational, centrifugal distortion, and quadrupole coupling constants are listed in Table 3. It is intended to investigate further isotopomers. In Fig. 1 a typical recording of an observed rotational transition is displayed. It should be mentioned that the *a*-type rotational spectrum of BZN is modified to an *a*- and *b*-type spectrum of the cluster, as the permanent dipole moment

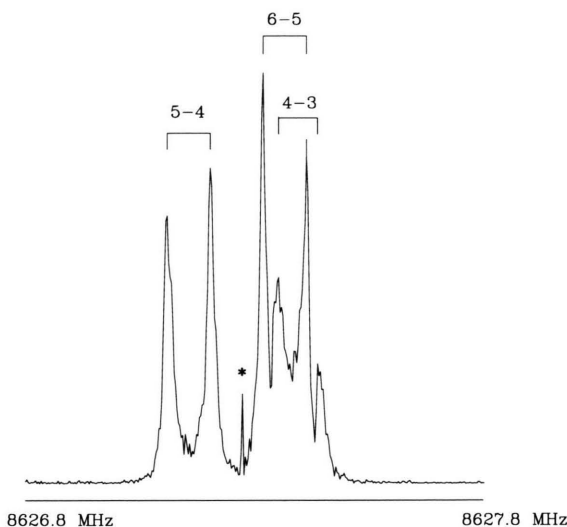


Fig. 1. Rotational transition  $J_{K_a K_c} = 5_{24} - 4_{23}$  of BZNW showing  $^{14}\text{N}$ -hfs. 16 K data points were recorded with a sample interval of 40 ns and 6 K averaging cycles. As carrier gas He, saturated with  $\text{H}_2\text{O}$ , has been used. Backing pressure 120 kPa. The star (\*) indicates a coherent perturbation at the polarisation frequency of 8627.27 MHz.

of BZN is differently oriented in the principal inertia axis system of the cluster. This allows the determination of all rotational constants of the ground state  $S_0$  with roughly the same precision. Unfortunately this precision can usually not be transferred to the structure. In the case of weakly bound complexes the problem is further complicated by the occurrence of large amplitude motions.

#### B) Analysis of the UV Spectra

From the different cluster species present in the experiment only the ion current at the mass of 121 u, i. e. the mass of BZNW, is selected. In Fig. 2 the ion signal is plotted against the laser frequency between  $36442.25\text{ cm}^{-1}$  and  $36444.0\text{ cm}^{-1}$ . The ionization laser wavelength was fixed at 470 nm. The measured spectrum of the vibrationless  $S_1 \leftarrow S_0$  transition has two broad wings with a hole in the center, as is typical for *a*- and *b*-type transitions with a P- and R-branch and missing Q-branch, as discussed qualitatively above.

To determine the rotational constants we performed a fit of the measured spectrum to the rigid asymmetric rotor dipole transition [33] using the method of Correlation Automated Rotational Fitting (CARF) [3]. The technique determines the crosscorrelation between

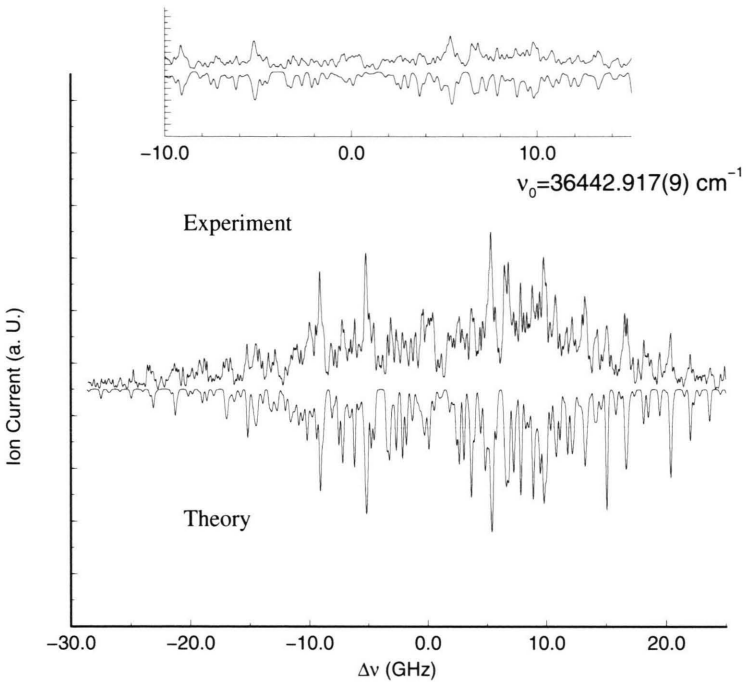


Fig. 2. Highly resolved UV spectrum of BZNW:  $S_1 \leftarrow S_0, 0_0^0$  transition. Upright traces: experimental spectrum. Inverted traces: calculated spectrum using the rotational constants found in this work by Correlation Automated Rotational Fitting. Top: magnified central part of the spectrum.

Table 1. Observed rotational MW transitions of BZNW ( $^{16}\text{O}$ ).

$\begin{smallmatrix} J'_{K'_a K'_c} \\ -J_{K_a K_c} \end{smallmatrix}$	$F'-F$	obs. [MHz]	obs.-calc. [kHz]	$\begin{smallmatrix} J'_{K'_a K'_c} \\ -J_{K_a K_c} \end{smallmatrix}$	$F'-F$	obs. [MHz]	obs.-calc. [kHz]	$\begin{smallmatrix} J'_{K'_a K'_c} \\ -J_{K_a K_c} \end{smallmatrix}$	$F'-F$	obs. [MHz]	obs.-calc. [kHz]
$1_{01}-0_{00}$	0-1	1737.6768	-0.3	$4_{13}-3_{12}$	3-2	7402.3240	1.9	$6_{33}-5_{32}$	5-4	10590.9892	-0.4
	1-1	1735.4873	-0.6		4-3	7402.2281	-1.0		6-5	10590.6932	0.4
	2-1	1736.3642	0.8		5-4	7402.3462	-1.7		7-6	10590.9491	-0.3
$2_{12}-1_{11}$	1-0	3218.2096	-5.6	$5_{05}-4_{04}$	4-3	8251.4835	-1.0	$7_{07}-6_{06}$	6-5	11199.3575	-4.6
	1-1	3217.3996	-6.8		5-4	8251.4948	-1.0		8-7	11199.3849	-0.5
	2-1	3216.4832	-2.8		6-5	8251.5368	4.2	$8_{18}-7_{17}$	8-7	12534.3060	-0.3
$2_{02}-1_{01}$	1-0	3447.5268	1.5	$5_{15}-4_{14}$	5-4	7951.1171	3.2		7-6	12534.3171	2.5
	1-1	3449.7169	2.4		6-5	7951.1853	0.5		9-8	12534.3328	0.6
	2-2	3447.3633	-0.7	$5_{23}-4_{22}$	4-3	9056.2556	-1.6	$7_{16}-6_{15}$	6-5	12640.3832	-2.2
	3-2	3448.3129	0.9		5-4	9056.0449	-1.9		7-6	12640.3569	-5.1
$2_{11}-1_{10}$	1-0	3728.8425	5.1		6-5	9056.2324	-5.0		8-7	12640.4046	4.0
	2-1	3726.9211	3.2	$5_{24}-4_{23}$	4-3	8627.3872	-1.0	$7_{25}-6_{24}$	6-5	12913.4950	-0.8
	3-2	3727.8213	4.9		5-4	8627.1526	-1.6		7-6	12913.4367	1.1
$3_{13}-2_{12}$	3-2	4811.1700	0.5		6-5	8627.3656	-0.8	$7_{25}-6_{24}$	8-7	12913.5048	2.5
	4-3	4811.4389	1.2	$5_{32}-4_{31}$	4-3	8779.9787	-1.4	$9_{09}-8_{08}$	8-7	14112.9428	1.6
$3_{22}-2_{21}$	2-1	5209.3749	0.2		5-4	8779.4263	-1.1		9-8	14112.9351	-0.3
	3-2	5207.9154	0.2		6-5	8779.8693	-1.5		10-9	14112.9569	1.5
	4-3	5208.8559	2.6	$5_{33}-4_{32}$	4-3	8750.3047	-2.2	$8_{17}-7_{16}$	7-6	14262.0160	-0.5
$3_{12}-2_{11}$	2-1	5575.6426	-3.2		5-4	8749.7466	-4.5		8-7	14261.9933	-1.0
	3-2	5575.3629	-4.0		6-5	8750.1960	-1.1		9-8	14262.0293	1.0
	4-3	5575.6243	-2.1	$6_{06}-5_{05}$	5-4	9738.2494	0.2	$1_{11}-0_{00}$	0-1	3622.2448	-1.6
$4_{14}-3_{13}$	3-2	6390.0616	0.3		7-6	9738.2842	3.0		1-1	3623.0525	-2.7
	4-3	6389.9856	-0.4	$6_{16}-5_{15}$	5-4	9494.3880	0.1		2-1	3622.7316	-0.1
	5-4	6390.1101	0.7		6-5	9494.3693	-0.8	$2_{12}-1_{01}$	1-0	5102.7873	2.8
$4_{23}-3_{22}$	3-2	6926.1923	0.1		7-6	9494.4178	1.0		2-1	5104.0508	-2.5
	4-3	6925.6901	1.2	$6_{24}-5_{23}$	5-4	10985.3177	-0.5		3-2	5103.7746	5.5
	5-4	6926.0917	2.3		6-5	10985.2125	0.7	$8_{08}-7_{17}$	7-6	12348.0838	-6.6
$4_{22}-3_{21}$	3-2	7155.8747	0.8	$6_{25}-5_{24}$	6-5	10308.9217	3.8		9-8	12348.1123	4.4
	4-3	7155.3954	2.8		7-6	10309.0450	-1.5	$8_{18}-7_{07}$	7-6	12840.5584	-6.6
	5-4	7155.7769	3.2	$6_{34}-5_{33}$	5-4	10513.7101	2.0		9-8	12840.5859	3.0
					6-5	10513.4126	6.6	$6_{25}-5_{14}$	5-4	14555.2054	-7.2
					7-6	10513.6685	1.3		6-5	14555.3056	2.7
									7-6	14555.2539	4.5



Table 2. Observed rotational MW transitions of BZNW (<sup>18</sup>O).

$J'_{K'_a K'_c} - J_{K_a K_c}$	$F' - F$	obs. [MHz]	obs.-calc. [kHz]	$J'_{K'_a K'_c} - J_{K_a K_c}$	$F' - F$	obs. [MHz]	obs.-calc. [kHz]	$J'_{K'_a K'_c} - J_{K_a K_c}$	$F' - F$	obs. [MHz]	obs.-calc. [kHz]
$1_{01}-0_{00}$	0-1	1673.6900	1.8	$6_{16}-5_{15}$	5-4	9164.3238	3.8	$9_{09}-8_{08}$	9-8	13635.6381	-3.2
	1-1	1671.5936	-1.9		6-5	9164.2980	-3.5		10-9	13635.6688	4.8
	2-1	1672.4345	2.0		7-6	9164.3529	4.4		0-1	3539.8599	0.1
$2_{12}-1_{11}$	1-0	3103.7490	-3.0	$6_{06}-5_{05}$	6-5	9407.7618	0.9	$1_{11}-0_{00}$	1-1	3540.5615	0.0
	2-1	3102.1168	-6.1		7-6	9407.7939	-5.1		2-1	3540.2844	3.5
	3-2	3102.9976	-1.8		6-5	9935.1665	-2.9		4-3	8717.9225	-4.3
$2_{02}-1_{01}$	1-0	3321.9131	1.0	$6_{25}-5_{24}$	7-6	9935.2953	1.2	$5_{15}-4_{04}$	5-4	8717.9414	3.3
	1-1	3323.9972	-7.6		6-5	10558.8163	2.8		6-5	8717.9742	0.6
	2-2	3321.7520	-0.4		7-6	10558.9115	0.4		2-1	10620.6903	0.2
$2_{11}-1_{10}$	2-1	3322.5946	5.2	$7_{17}-6_{16}$	6-5	10640.1714	-1.8	$3_{22}-2_{11}$	3-2	10621.1614	3.2
	3-2	3322.6620	-0.1		7-6	10640.1623	1.8		4-3	10620.8590	1.6
	1-0	3587.5120	5.7		8-7	10640.1986	3.5		8-7	11901.6691	-2.3
$5_{05}-4_{04}$	2-1	3585.6492	1.7	$7_{16}-6_{15}$	6-5	12185.5701	-2.6	$8_{08}-7_{07}$	9-8	11901.7002	4.9
	3-2	3586.5059	1.5		7-6	12185.5418	-2.5		7-6	12428.4536	-1.2
	5-4	7967.6944	-1.8		8-7	12185.5898	3.9		8-7	12428.4370	-4.1
$5_{24}-4_{23}$	6-5	7967.7407	1.9	$8_{08}-7_{07}$	7-6	12227.2706	-0.2	$4_{22}-3_{13}$	9-8	12428.4742	2.6
	4-3	8312.6551	6.4		8-7	12227.2586	-1.9		3-2	13695.1220	2.1
	5-4	8312.4251	1.6		9-8	12227.2887	0.7		4-3	13695.8621	-2.4
$5_{14}-4_{13}$	6-5	8312.6262	-1.5	$9_{19}-8_{18}$	9-8	13555.1285	1.1		5-4	13695.3307	-4.7
	4-3	8855.8733	-8.6		10-9	13555.1535	4.3				
	5-4	8855.8381	3.6								
	6-5	8855.9035	0.1								

Table 3. Experimental rotational, van Eijck [44] centrifugal distortion, and quadrupole coupling constants of the BZNW complex. Moments of inertia  $I_g$ , inertia defect  $\Delta$ , and planar moments  $P_g$  (conversion factor  $5.05376 \cdot 10^5$  MHz amu Å<sup>2</sup> [39]),  $\kappa$  Ray-asymmetry parameter,  $N$  number of hyperfine components,  $\sigma$  standard deviation.

	H <sub>2</sub> <sup>16</sup> O (S <sub>0</sub> )	H <sub>2</sub> <sup>18</sup> O (S <sub>0</sub> )	H <sub>2</sub> <sup>16</sup> O (S <sub>1</sub> )
$A$ /MHz	2882.2886(22)	2825.0638(44)	2821.6(23)
$B$ /MHz	995.71865(39)	957.02927(41)	984.3(14)
$C$ /MHz	740.49971(23)	715.26447(24)	729.0(33)
$\kappa$	-0.7617	-0.7706	-0.756(3)
$D'_J$ /kHz	0.2576(15)	0.2598(25)	
$D''_J$ /kHz	-0.678(16)	-0.763(57)	
$D'_K$ /kHz	4.21(45)	4.54(80)	
$\delta'_J$ /kHz	0.0874(16)	0.0861(20)	
$R'_6$ /kHz	-0.0097(11)	-0.0092(22)	
$\chi_{aa}$ /MHz	-2.9196(29)	-2.7904(33)	
$\chi_{bb}$ /MHz	1.0824(53)	0.936(13)	
$\chi_{cc}$ /MHz	1.8372(53)	1.854(13)	
$\sigma$ /kHz	3.2	3.6	CARF
$N$	69	58	CARF
$I_a$ /amu Å <sup>2</sup>	175.338	178.890	179.1(2)
$I_b$ /amu Å <sup>2</sup>	507.549	528.068	513.4(7)
$I_c$ /amu Å <sup>2</sup>	682.480	706.559	693.2(31)
$P_a$ /amu Å <sup>2</sup>	507.346	527.869	513.8(16)
$P_b$ /amu Å <sup>2</sup>	175.135	178.691	179.4(16)
$P_c$ /amu Å <sup>2</sup>	0.219	0.200	-0.4(16)
$\Delta$ /amu Å <sup>2</sup>	-0.407	-0.399	0.7(32)
Origin/cm <sup>-1</sup>			36442.917(9)

experiment and simulation. The position of the cross-correlation peak defines the relative position of experimental and simulated spectrum and therefore the origin of the transition. The height of the crosscorrelation peak is a criterion for the quality of the simu-

lation and is adapted sequentially in a fit procedure. This is the first demonstration of this technique for complex spectra. The S<sub>0</sub> rotational constants were taken from the MW experiments in the previous section and not changed during the fit. The fit was started with the ground state values for both electronic states and relative intensities of *a*- and *b*-type transitions of 30 to 70. After the exact microwave data was available we assumed that the orientation change of the transition moment upon clustering is negligible and therefore the new orientation of the BZN monomer *b*-axis, which can be found from the orthogonal transformation matrix in Table 6, defines the orientation of the transition moment in the cluster. This means an intensity ratio of *a*- to *b*-type of 19 to 81 and an orientation of the transition moment of 26° with respect to the principal *b*-axis of the cluster.

In Table 3 the rotational constants resulting from the fit are given together with the MW data. The error of the rotational constants is given by the standard deviation of the fits of 12 separately measured experimental spectra of the band and additionally it is ensured that the visual agreement between experimental and theoretical spectrum decreases noticeably when leaving the error bars. In the lower inverted trace of Fig. 2 the spectrum calculated for a rotational temperature of 1.0 K with the constants of Table 3 is shown representing the best agreement with the measured spectrum. The agreement of line positions

Table 4. UV linewidth of BZN monomer for several clustering partners.

Molecule/Cluster	Linewidth [MHz]
C <sub>6</sub> H <sub>5</sub> CN	<100 <sup>a</sup>
C <sub>6</sub> H <sub>5</sub> CN·Ar	150 <sup>a</sup>
C <sub>6</sub> H <sub>5</sub> CN·H <sub>2</sub> O	180 <sup>b</sup>
C <sub>6</sub> H <sub>5</sub> CN·(H <sub>2</sub> O) <sub>2</sub>	unresolved <sup>c</sup>

<sup>a</sup> [3]; <sup>b</sup> this work; <sup>c</sup> [34].

in the central part of the spectrum is demonstrated in the inset of Fig. 2 with a magnified part of the spectrum. A further fit of intensities which could include a two temperature model, saturation, intensity dependent noise, constant ground noise and different dipole transition moment orientations could result in a better optical agreement of theory and experiment in Fig. 2 but would not change the accuracy of the inertial constants. This has been verified in a series of fits performed in addition to the one shown in Figure 2.

For the presentation the calculated stick spectrum was convoluted with a Gaussian line shape of 180 MHz (FWHM) to match the resolution in the experimental spectrum. The observed linewidth of 180 MHz is larger than expected from the experimental resolution. An increasing line broadening is observed for a series of spectra: for unchanged experimental conditions we observed a linewidth of the BZN monomer of less than 100 MHz (instrumental resolution), a linewidth of the BZN·Ar complex of 150 MHz [3] and in this work of the BZNW of 180 MHz. Furthermore, measurements of the BZN·(H<sub>2</sub>O)<sub>2</sub> cluster [34] show an unresolved rotational structure. The lifetimes are summarized in Table 4. There are several possible explanations for these results: Line broadening due to saturation, to unresolved line splitting or to fast decay dynamics. Since the expansion conditions were not changed in the series of the experiments and the laser intensity was optimized for highest spectral resolution, saturation as a source of the broadening seems to be unlikely. A line splitting due to the torsional motion of the water moiety may be below the experimental resolution and thus could lead to a broadening of the observed linewidth. This, however, would not explain the line broadening observed in BZN·Ar. Therefore the most reasonable explanation for the observed line broadening is a decreasing lifetime with increasing cluster size and/or polarity of the solvent. The lifetime of the electronically excited S<sub>1</sub> state decreases with the number and/or the

dipole moment of the clustering partners. Ultra short time-resolved and highly resolved dispersed fluorescence experiments may clarify whether the excited electronic states in these species decay to the electronic ground state, to the proposed charge transfer state [11, 12] or whether a fragmentation of the clusters occurs.

Comparing these results for the dynamics with other aromatic water clusters like phenol-water we found that BZNW decays faster upon clustering, whereas phenol-water has a longer lifetime than pure phenol [6]. This may be due to the different nonradiative processes responsible for the dynamics in the two systems.

### C) Cluster Structure

First the analysis of the MW data is reported. We assumed in all structural calculations in the S<sub>0</sub> state that the structure of BZN [4, 35] and water [36] is invariant under complexation. Despite of its approximate character this assumption has proved to be a reasonable one for the vibronic ground state if one is mainly interested in the determination of intermolecular structural parameters [37]. However, we think that internal structural changes are expected to be smaller than e. g. in phenol-water or pyridone-water [23, 8] since the bonding is weaker and the bond length is longer in BZNW.

The numbering of the atoms is given in Figure 3. The planar moment  $P_c$  or the inertial defect [38] indicates that the cluster is nearly planar. Assuming near planarity for the cluster the number of independent rotational constants is practically reduced to four. Taking O is situated nearly in the BZN plane the main contribution to the inertial defect comes from the water hydrogens. In a  $r_0$  calculation (program ru111 [39, 40]) we fitted the six moments of inertia by varying two in plane parameters i) the “bond” distance  $r$ , H<sub>2</sub>-O and ii) the angle  $\beta$ , (C<sub>2</sub>H<sub>2</sub>O); additional parameters were also fitted which change the out of plane positions of the water hydrogens in order to account for the experimentally determined inertial defect. The fitting of out of plane parameters will be described in more detail in the following.

In a first calculation the inclination  $\gamma$  of the symmetry axis of water with respect to the BZN plane was additionally fitted (see Fig. 3 for illustration). The atoms H<sub>a</sub> and H<sub>b</sub> move above (below) and O below (above) the (a,b)-plane of the complex whereas the

Table 5. Structure parameters of the cluster obtained with an  $r_0$ -fit. For definition of  $\beta$  and  $\gamma$  see text and Figure 3. Derived parameters below the first line.  $\Delta I_g = I_{g_{exp}} - I_{g_{calc}}$ ,  $g = a, b, c$  in  $S_0$  mean value for the  $^{16}\text{O}$  and  $^{18}\text{O}$  isotopomers.

	$S_0$ (MW)	$S_1$ (UV)
$r(\text{H}_2\text{-O})[\text{\AA}]$	2.477(4)	2.457(2)
$\beta$ ( $\angle(\text{C}_2, \text{H}_2, \text{O})$ ) [ $^\circ$ ]	143.34(2)	141.91(3)
$\gamma$ [ $^\circ$ ]	33.7(60)	0
$r(\text{CM}(\text{B})\text{-CM}(\text{W}))[\text{\AA}]$	4.152(3)	4.155
$r(\text{H}_a\text{-N})[\text{\AA}]$	2.612(16)	2.631
$ \Delta I_a [\text{amu \AA}^2]$	0.0017	0.05
$ \Delta I_b [\text{amu \AA}^2]$	0.0002	0.90
$ \Delta I_c [\text{amu \AA}^2]$	0.007	0.64

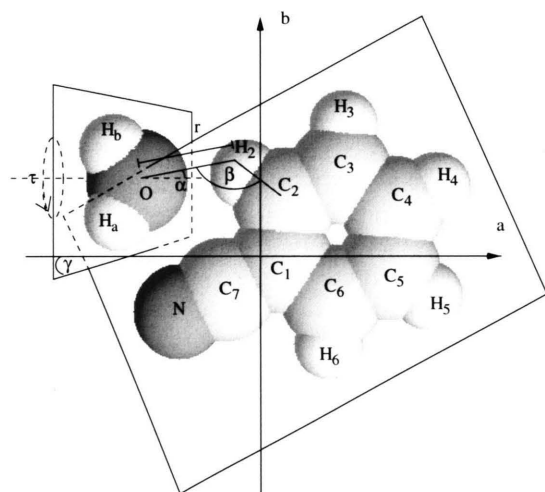


Fig. 3. Experimentally obtained structure of the BZNW complex. Numbering and geometric parameters, see text. Only the structure with the torsion angle  $\tau = 0$  is shown.  $\gamma$  describes the inclination of the water plane with respect to the BZN plane.

center of mass of  $\text{H}_2\text{O}$  stays in the plane. The results are given in Table 5. A significant torsion angle  $\tau$  about the water symmetry axis could not be determined in this calculation. The fitting procedure showed an oscillating behavior around zero.

In Table 6 we give the coordinates of the atoms in the principal axis system of the cluster for  $\tau = 0$ . The adjustment of the parameters  $r$ ,  $\beta$ ,  $\gamma$  exhausts the information of the six moments of inertia in this calculation.

In a second calculation we tried to adjust  $r$ ,  $\beta$ ,  $\tau$  and the angle  $\alpha$  between the water symmetry axis and

Table 6. Top: cartesian coordinates  $a_0$ ,  $b_0$ ,  $c_0$  of the atoms of the  $^{16}\text{O}$  BZNW complex in its principal axes system. They resulted from an  $r_0$  fit of the moments of inertia of the  $^{16}\text{O}$  and the  $^{18}\text{O}$  isotopomers with the  $r_0$ -structure of BZN  $S_0$  [27, 35] and  $S_1$  [3] and the assumed structure of water [36]. CM(B) and CM(W) center of mass of BZN and water, respectively. Uncertainty of the last digit is given in parentheses, these errors do not include the errors of the method. Middle: orthogonal transformation matrix between the principal axis systems of BZN and the complex. Bottom:  $r_s$ -coordinates  $a_s$ ,  $b_s$ ,  $c_s$  of O in  $S_0$  for comparison, error estimate according to [45]. UV data based on modeling calculation of [3].

Atom (No)	$S_0$			$S_1$		
	$a_0[\text{\AA}]$	$b_0[\text{\AA}]$	$c_0[\text{\AA}]$	$a[\text{\AA}]$	$b[\text{\AA}]$	$c[\text{\AA}]$
N	-2.2514(1)	-1.6136(3)	0.0082(13)	-2.28	-1.61	0
C1	0.0854(0)	-0.4737(1)	0.0027(4)	0.05	-0.49	0
C2	0.1688(1)	0.9218(1)	0.0092(13)	0.15	0.94	0
C3	1.4254(2)	1.5274(0)	0.0062(9)	1.44	1.56	0
C4	2.5912(1)	0.7486(1)	-0.0033(6)	2.62	0.75	0
C5	2.4873(0)	-0.6496(1)	-0.0097(15)	2.52	-0.68	0
C6	1.2364(1)	-1.2671(0)	-0.0068(10)	1.23	-1.30	0
C7	-1.2124(1)	-1.1068(2)	0.0057(9)	-1.23	-1.10	0
H2	-0.7365(2)	1.5126(2)	0.0165(24)	-0.74	1.54	0
H3	1.5018(3)	2.6057(0)	0.0113(16)	1.52	2.63	0
H4	3.5619(1)	1.2220(2)	-0.0055(10)	3.60	1.22	0
H5	3.3841(1)	-1.2532(2)	-0.0171(26)	3.41	-1.28	0
H6	1.1448(2)	-2.3442(0)	-0.0118(18)	1.15	-2.37	0
O	-3.2090(36)	1.3598(7)	0.0276(42)	-3.20	1.38	0
H <sub>a</sub>	-3.653(28)	0.5681(20)	-0.301(44)	-3.73	0.58	0
H <sub>b</sub>	-3.747(28)	2.094(19)	-0.293(43)	-3.83	2.09	0
CM (B)	0.5705(0)	-0.2371(1)	0.0015(2)	0.57	-0.24	0
CM (W)	-3.2636(3)	1.3567(5)	-0.0085(12)	-3.26	1.37	0
Transformation matrix	$\begin{pmatrix} 0.899121 & 0.437690 & 0.002880 \\ -0.437632 & 0.899078 & -0.116949 \\ -0.007708 & 0.009255 & 0.999928 \end{pmatrix}$			$\begin{pmatrix} 0.901 & 0.435 & 0 \\ -0.435 & 0.901 & 0 \\ 0 & 0 & 1 \end{pmatrix}$		
Atom (No)	$ a_s [\text{\AA}]$	$ b_s [\text{\AA}]$	$ c_s [\text{\AA}]$			
O (14)	3.2092(2)	1.3839(4)	imaginary			

the  $\text{H}_2\text{-O}$  direction, see Figure 3. These parameters could be determined, but the resulting  $\Delta I_g$  were by an order of magnitude worse.

In a third calculation we adjusted  $r$  and  $\beta$ , kept the  $\text{O-H}_a$  bond directed towards N in the plane and rotated the  $\text{O-H}_b$  bond about the  $\text{O-H}_a$  bond out of the plane. The angle  $\alpha' = \angle(\text{H}_2, \text{O}, \text{H}_a)$ , i.e. the angular position of the water subunit, was also adjusted. In this case a fit of the moments of inertia can be obtained with a quality similar to that reported in Table 5, now with one hydrogen elevated  $0.435 \text{ \AA}$  out of the  $a, b$ -plane and  $\alpha' = 108.51^\circ$ .

These calculations show that the position and orientation of water can be changed and the moments of inertia are still reproduced reasonably. But they also confirm that the information provided by the six moments of inertia is not sufficient to fix the six structural

parameters necessary to describe the position and orientation of water unequivocally.

As the moments of inertia depend on the squares of the coordinates, other geometries cannot in fact be excluded. A possible near planar structure has the oxygen O approaching 1.1 Å to the meta hydrogen H<sub>3</sub>. This is an unlikely structure for intracuster bonds.

As the <sup>16</sup>O- and <sup>18</sup>O-isotopomers were investigated the position of the O atom in the principal axis system of the <sup>16</sup>O-isotopomer can be calculated by the  $r_s$  method [41]. The  $r_s$  coordinates are given at the end of Table 6. The coordinates  $a_s$  and  $b_s$  agree reasonably with the  $r_0$  values and  $c_s$  results imaginary, which indicates a substitution near to the ( $a,b$ )-inertia plane.

The problem of the structure determination is not completely solved, yet. We are investigating the <sup>15</sup>N–BZNW isotopomers to get unequivocal information.

We observed further some  $b$ -type transitions showing narrow splittings in the order of several 10 kHz. This may indicate a torsional motion, this effect needs further detailed investigations. In Table 1 and 2 the frequencies of split lines are given by the arithmetic mean of the component frequencies.

The <sup>14</sup>N nuclear quadrupole coupling [30] may give some information on the complex structure. If the quadrupole coupling tensor of BZN  $\chi_{aa} = -4.2391(18)$  MHz,  $\chi_{bb} = 2.2893(32)$  MHz,  $\chi_{cc} = 1.9498(32)$  MHz [35] is transformed to the principal inertia system of the cluster determined by the  $r_0$  calculation, using the orthogonal matrix given in Table 6, one gets  $\chi'_{aa} = -2.9884$  MHz,  $\chi'_{bb} = 1.0384$  MHz,  $\chi'_{cc} = 1.9495$  MHz. These values differ from the  $\chi_{gg}$  of Table 3, as the N-H<sub>a</sub> “bond” may influence the electronic surrounding of N. The  $\chi'_{gg}$  may not be used as an argument against near planarity of the complex. The nuclear quadrupole coupling constants  $\chi_{gg}$  do not exclude a second configuration, as mentioned above, since the angle between the C<sub>2</sub> axis of BZN and the  $a$  inertia axis is close to that one of the first configuration.

The UV data is interpreted in a similar way: The inertial tensor of the complex is calculated by transforming the inertial tensor of the water molecule [36] to a representation in the S<sub>1</sub> BZN center of mass coordinate representation [3] and by summation according Steiner's law [42]. We performed a calculation of the rotational constants for different cluster structures and compared them with rotational constants obtained from the experimental data in a fit procedure of the

cluster structure using a conjugate gradient algorithm [43]. Since only the relative positioning of the two centers of mass results in a relevant change of the inertial tensor, different fits were performed for  $\tau = 0^\circ$  and  $\tau = 90^\circ$ .  $\alpha$  was fixed so that the water symmetry axis was orientated towards the hydrogen in ortho position H<sub>2</sub> (hereafter called ortho hydrogen) and  $\gamma$  was set to  $0^\circ$ . The fit quality and the agreement of the inertial defect are much better for the in-plane configuration ( $\tau = 0^\circ$ ), but both configurations converge within the experimental error bar. For determination of the detailed localization of the water molecule in S<sub>1</sub> further isotope substituted measurements are desirable. To visualize the structural results of the fit we calculated the distances relative to the known position of the ortho hydrogen in S<sub>1</sub> [3]. These are summarized in Table 5 and Figure 3. The complete result of the fit is given in Table 6.

The bond length of  $r_0 = 2.477(4)$  Å is between the typical bond length of a van der Waals bonded (e. g. van der Waals bond length of BZN·Ar in S<sub>0</sub> (S<sub>1</sub>): 3.598 Å (3.52 Å) [3, 4]) and a hydrogen-bonded system (e. g. phenol·water: the distance from the phenol's hydrogen to the water's oxygen in S<sub>0</sub> (S<sub>1</sub>) is roughly 1.97 Å (1.93 Å) [6]). The two links of the water to the ortho hydrogen and the C–N group should be compared to recent findings in pyridone·water. In BZNW the distance of the water oxygen to the BZN ortho hydrogen in S<sub>0</sub> (S<sub>1</sub>) is 2.477 Å (2.46 Å), whereas the distance between the water hydrogen and the BZN nitrogen is 2.612 Å (2.63 Å). The respective distances in pyridone·water derived from the Kraitichman equations are smaller and increase upon electronic excitation: The distance of the water oxygen to the nearest pyridone hydrogen is 2.01 Å (2.05 Å), the water hydrogen is 1.97 Å (2.05 Å) apart from the pyridone oxygen [8]. This might be due to the different position of the H<sub>2</sub>O molecule in the two systems, with the nested character of the water position in BZNW and the side-on position in pyridone·water.

This shows that the bonding in the BZNW complex has hydrogen as well as van der Waals character. The calculation also shows that there are minor structure changes between S<sub>0</sub> and S<sub>1</sub> concerning the position of the water relative to the center of mass of the BZN molecule. The change of the intermolecular bond length upon electronic excitation is larger than the distance change between the centers of mass of the two molecules. The changes can be explained by the structure change from S<sub>0</sub> [4] to S<sub>1</sub> [3] of the BZN



monomer. This means that the intermolecular bonding is only slightly affected by the electronic excitation.

For comparison the changes of the bond length upon electronic excitation in complexes between aromatics and rare gases are larger. E.g. in benzene-Ar the Ar is located above the ring at a distance of 3.58 Å (3.52 Å)  $S_0$  ( $S_1$ ) [7]. The larger change of the bond distance after electronic excitation is caused by the influence of the  $\pi$ -electron excitation in the benzene ring on the van der Waals bonding due to the increasing polarizability in the electronically excited benzene. The in-plane side-on position of the water in BZNW is less influenced by the electronic  $\pi\pi^*$ -excitation localized in the ring. It is somewhat surprising that the attachment of the water does not change the structure of the electronically excited BZN. A still open question is in line with the proposed influence of the polar solvent water on the probability of charge transfer reactions. Further investigation of the vibrations in  $S_1$  is needed in order to interpret the consequences of this result on the influence of the polar solvent water on the excited state leading to TICT or RICT [11, 12] states.

#### IV. Summary and Conclusion

In this work we presented highly resolved spectra of the BZNW complex. The virtue of the special combination of MW and high resolution UV results yields information on the structure of this cluster between an aromatic molecule and water not only in the  $S_0$  ground state but also in the  $S_1$  excited state and demonstrates the effect of electronic  $\pi\pi^*$ -excitation on the structure and on the intermolecular bonding.

The technique of high resolution mass-resolved UV spectroscopy is applied for the first time to small hydrogen-bonded clusters yielding species-selective

information. The observed line broadening after clustering with the polar  $H_2O$  points to an influence of the polarity of the clustering partner on the linewidth. Further investigations will clarify this point.

A structure fit reveals that the water is located near the plane of the BZN molecule with one or two water hydrogens off the plane. For  $S_0$  ( $S_1$ ) the distance of the oxygen to the ortho hydrogen is  $r_0 = 2.477(4)$  Å (2.457(2) Å) and the angle to the ortho carbon-hydrogen bond  $143.34(2)^\circ$  ( $141.91(3)^\circ$ ). The measured structure changes of the cluster from  $S_0$  to  $S_1$  can be explained by the change of the structure of the BZN monomer itself. The position of the water relative to the ortho hydrogen is only slightly affected by the electronic excitation.

The MW investigation will be extended to more isotopomers to get a better determination of the six relative parameters for the water position and orientation.

Further high resolution UV measurements of intermolecular vibronic bands in  $S_1$  are supposed to yield information on the potential surface of the mixed van der Waals and hydrogen-bonding potential.

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